

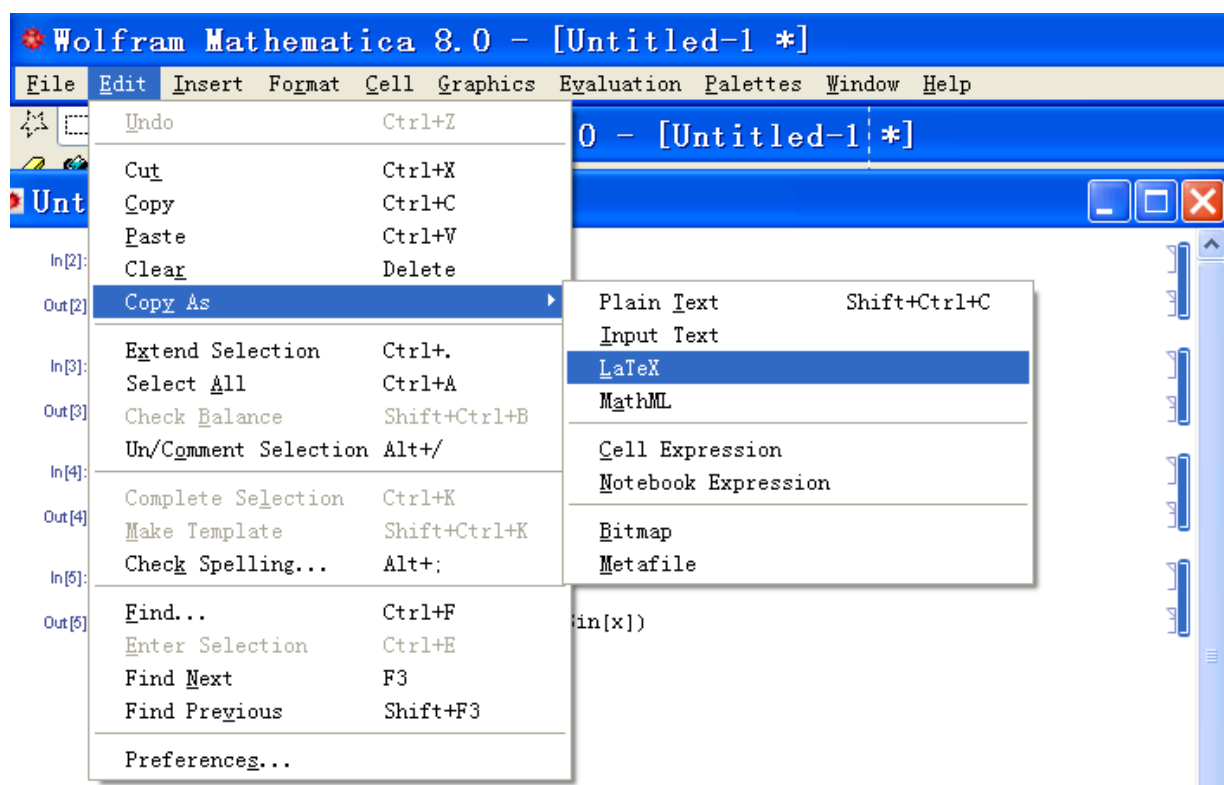
基于数学软件（Mathematica、Matlab 等）的 LaTeX 源程序生成

本讲要点：

- 一、Mathematica 与 LaTeX 源程序
- 二、Matlab 与 LaTeX 源程序
- 三、练习

一、Mathematica 与 LaTeX 源程序

Mathematica 软件直接基于符号运算，因此，可以利用它直接得到有关的 LaTeX 源程序。方法是：



例 1（简单应用）：已知 $f(x) = \sin^5(x)$ ，求 $f'''(x)$ 。

`D[Sin[x]^5,{x,3}]`

结果为： $60 \cos^3(x) \sin^2(x) - 65 \cos(x) \sin^4(x)$

选中上述细胞（cell），然后 Copy As LaTeX 格式，得到 LaTeX 源程序为：

`D[\text{Sin}[x]^{\wedge}5,\{x,3\}]`

60 $\text{Cos}[x]^3 \text{Sin}[x]^2 - 65 \text{Cos}[x] \text{Sin}[x]^4$

例 2 (较复杂应用): 已知 $f(x) = (\sin x)^{\cos x}$, 求 $f''(x)$.

`D[(Sin[x]^Cos[x]),{x,2}]`

结果为: $(-2 \text{Cos}[x] - \text{Cot}[x] \text{Csc}[x] - \text{Cos}[x] \text{Log}[\text{Sin}[x]]) \text{Sin}[x]^{\text{Cos}[x]} + \text{Sin}[x]^{\text{Cos}[x]} (\text{Cos}[x] \text{Cot}[x] - \text{Log}[\text{Sin}[x]] \text{Sin}[x])^2$

选中上述细胞 (cell), 然后 **Copy As LaTeX** 格式, 得到 **LaTeX** 源程序为:

`D[(\text{Sin}[x])^{\wedge}\{\text{Cos}[x],\{x,2\}}`

$(-2 \text{Cos}[x] - \text{Cot}[x] \text{Csc}[x] - \text{Cos}[x] \text{Log}[\text{Sin}[x]]) \text{Sin}[x]^{\text{Cos}[x]} + \text{Sin}[x]^{\text{Cos}[x]} (\text{Cos}[x] \text{Cot}[x] - \text{Log}[\text{Sin}[x]] \text{Sin}[x])^2$

也可使用自定义函数:

例 3 (较复杂应用): 已知 $f(x, y) = (\sin x)^{\cos y}$, 求 $\frac{\partial^3 f(x, y)}{\partial x^2 \partial y}$.

`myfun[x_,y_]:=Sin[x]^Cos[y]`

`D[myfun[x,y],{x,2},{y,1}]`

结果为:

$-\text{Cos}[x]^2 (-1 + \text{Cos}[y]) \text{Sin}[x]^{-2 + \text{Cos}[y]} \text{Sin}[y] - \text{Cos}[x]^2 \text{Cos}[y] \text{Sin}[x]^{-2 + \text{Cos}[y]} \text{Sin}[y] - \text{Cos}[x]^2 (-1 + \text{Cos}[y]) \text{Cos}[y] \text{Log}[\text{Sin}[x]] \text{Sin}[x]^{-2 + \text{Cos}[y]} \text{Sin}[y] + \text{Sin}[x]^{\text{Cos}[y]} \text{Sin}[y] + \text{Cos}[y] \text{Log}[\text{Sin}[x]] \text{Sin}[x]^{\text{Cos}[y]} \text{Sin}[y]$

选中上述细胞 (cell), 然后 **Copy As LaTeX** 格式, 得到 **LaTeX** 源程序为:

`\text{myfun}[\text{x}_\$, \text{y}_\$]\text{:=}\text{Sin}[x]^{\wedge}\{\text{Cos}[y]`

`D[\text{myfun}[x,y],\{x,2\},\{y,1\}]`

$-\text{Cos}[x]^2 (-1 + \text{Cos}[y]) \text{Sin}[x]^{-2 + \text{Cos}[y]} \text{Sin}[y] - \text{Cos}[x]^2 \text{Cos}[y] \text{Sin}[x]^{-2 + \text{Cos}[y]} \text{Sin}[y] - \text{Cos}[x]^2 (-1 + \text{Cos}[y]) \text{Cos}[y] \text{Log}[\text{Sin}[x]] \text{Sin}[x]^{-2 + \text{Cos}[y]} \text{Sin}[y] + \text{Sin}[x]^{\text{Cos}[y]} \text{Sin}[y] + \text{Cos}[y] \text{Log}[\text{Sin}[x]] \text{Sin}[x]^{\text{Cos}[y]} \text{Sin}[y]$

例 4 (复杂应用): 已知 $f(x) = x^{x^{x^x}}$, 求 $f'''(x)$.

(1) Mathematica 命令:

`D[x^x^x^x,{x,3}]` (或 `D[x^(x^(x^x)),{x,3}]`)

(2) Mathematica 结果:

$x^{x^x} (x^{-1+x^x} + x^{x^x} \text{Log}[x] (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x]))) + 3 x^{x^x} (x^{-1+x^x} + x^{x^x} \text{Log}[x] (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x]))) (x^{-1+x^x} (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x])) + x^{x^x} \text{Log}[x] (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x]))) + 2 x^{-1+x^x} ((-1 + x^x) / x + x^x \text{Log}[x] (1 + \text{Log}[x])) + x^{x^x} \text{Log}[x] (x^{-1+x} \text{Log}[x] + x^{-1+x} (1 + \text{Log}[x]) + x^x \text{Log}[x] (1 + \text{Log}[x])) + 2 x^{-1+x} ((-1+x) / x + \text{Log}[x]) + x^{x^x} (x^{-1+x^x} (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x])) + 2 x^{x^x} \text{Log}[x] (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x]))) + x^{x^x} \text{Log}[x] (x^{-1+x^x} (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x])) + 2 x^{x^x} \text{Log}[x] (x^{-1+x} + x^x \text{Log}[x] (1 + \text{Log}[x])))$

$$\begin{aligned}
& x^{x^{x^x}} \left(x^{-1+x^x} + x^{x^x} \ln(x) \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) \right)^3 + \\
& 3x^{x^{x^x}} \left(x^{-1+x^x} + x^{x^x} \ln(x) \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) \right) \\
& \left(x^{-1+x^x} \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) + x^{x^x} \ln(x) \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) \right)^2 + \\
& x^{-1+x^x} \left(\frac{-1+x^x}{x} + x^x \ln(x)(1 + \ln(x)) \right) + \\
& x^{x^x} \ln(x) \left(x^{-1+x} \ln(x) + x^{-1+x}(1 + \ln(x)) + x^x \ln(x)(1 + \ln(x)) \right)^2 + \\
& x^{-1+x} \left(\frac{-1+x}{x} + \ln(x) \right) \Big) + \\
& x^{x^{x^x}} \left(x^{-1+x^x} \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) \right)^2 + x^{x^x} \ln(x) \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right)^3 + \\
& x^{-1+x^x} \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) \left(\frac{-1+x^x}{x} + x^x \ln(x)(1 + \ln(x)) \right) + \\
& x^{-1+x^x} \left(\frac{-1+x^x}{x} + x^x \ln(x)(1 + \ln(x)) \right)^2 + \\
& x^{-1+x^x} \left(-\frac{-1+x^x}{x^2} + x^{-1+x} \ln(x) + 2x^{-1+x}(1 + \ln(x)) + x^x \ln(x)(1 + \ln(x))^2 \right) + \\
& 2x^{-1+x^x} \left(x^{-1+x} \ln(x) + x^{-1+x}(1 + \ln(x)) + x^x \ln(x)(1 + \ln(x)) \right)^2 + \\
& x^{-1+x} \left(\frac{-1+x}{x} + \ln(x) \right) \Big) + 3x^{x^x} \ln(x) \left(x^{-1+x} + x^x \ln(x)(1 + \ln(x)) \right) \\
& \left(x^{-1+x} \ln(x) + x^{-1+x}(1 + \ln(x)) + x^x \ln(x)(1 + \ln(x))^2 + x^{-1+x} \left(\frac{-1+x}{x} + \ln(x) \right) \right) \Big) + \\
& x^{x^x} \ln(x) \left(2x^{-2+x} + \left(-\frac{-1+x}{x^2} + \frac{2}{x} \right) x^{-1+x} + 2x^{-1+x} \ln(x)(1 + \ln(x)) + \right. \\
& \left. x^{-1+x}(1 + \ln(x))^2 + x^x \ln(x)(1 + \ln(x))^3 + x^{-1+x} \ln(x) \left(\frac{-1+x}{x} + \ln(x) \right) \right) + \\
& \left. x^{-1+x}(1 + \ln(x)) \left(\frac{-1+x}{x} + \ln(x) \right) + x^{-1+x} \left(\frac{-1+x}{x} + \ln(x) \right)^2 \right) \Big)
\end{aligned}$$

二、Matlab 与 LaTeX 源程序

Matlab 软件也有符号运算功能，可以利用它得到有关的 LaTeX 源程序，方法是利用 Matlab 的转换函数 latex (···)。Matlab 给出的帮助文件如下：

```
>> help latex
--- help for sym/latex.m ---
```

LATEX LaTeX representation of a symbolic expression.

LATEX(S) returns the LaTeX representation of the symbolic expression S.

Examples:

```
syms x
f = taylor(log(1+x));
latex(f) =
    x-1/2\, \{x\}^{\{2\}}+1/3\, \{x\}^{\{3\}}-1/4\, \{x\}^{\{4\}}+1/5\, \{x\}^{\{5\}}
```

```
H = sym(hilb(3));
latex(H) =
```

```
\left [\begin {array} {ccc} 1&1/2&1/3\\\noalign{\medskip}1/2&1/3&1/4
\\\noalign{\medskip}1/3&1/4&1/5\end {array}\right ]
```

```
syms alpha t
A = [alpha t alpha*t];
latex(A) =
\left [\begin {array} {ccc} \alpha&t&\alpha\,t\end {array}\right ]
```

See also pretty, ccode, fortran.

例 5 (简单应用): 已知 $f(x) = \sin^5(x)$, 求 $f'''(x)$.

```
>> syms x
>> latex(diff(sin(x)^5, x, 3))
```

得到的 LaTeX 命令为:

```
60\, \left( \sin \left( x \right) \right) ^{2} \left( \cos \left( x \right)
\right) ^{3}-65\, \left( \sin \left( x \right) \right) ^{4} \cos \left( x \right)
```

例 6 (较复杂应用): 已知 $f(x) = (\sin x)^{\cos x}$, 求 $f''(x)$.

```
>> syms x
>> latex(diff(sin(x)^cos(x), x, 2))
```

得到的 LaTeX 命令为:

```
\left( \sin \left( x \right) \right) ^{\cos \left( x \right) } \left( -\sin
\left( x \right) \ln \left( \sin \left( x \right) \right) +{\frac { \left( \cos
\left( x \right) \right) ^{2} }{\sin \left( x \right) }} \right) ^{2}+ \left( \sin
\left( x \right) \right) ^{\cos \left( x \right) } \left( -\cos \left( x \right)
\ln \left( \sin \left( x \right) \right) -3\, \cos \left( x \right) -{\frac
{ \left( \cos \left( x \right) \right) ^{3} }{\left( \sin \left( x \right)
\right) ^{2}}} \right)
```

也可使用自定义函数:

例7 (较复杂应用): 已知 $f(x, y) = (\sin x)^{\cos y}$, 求 $\frac{\partial^3 f(x, y)}{\partial x^2 \partial y}$.

```
>> syms x y
>> myfun = sin(x)^cos(y);
>> result= diff(diff(myfun, x, 2), y)
>> latex(result)
```

Matlab 的结果为:

```
-sin(x)^cos(y)*sin(y)*log(sin(x))*cos(y)^2*cos(x)^2/sin(x)^2-2*sin(x)^cos(y)
*cos(y)*cos(x)^2/sin(x)^2*sin(y)+sin(x)^cos(y)*sin(y)*log(sin(x))*cos(y)+sin
(x)^cos(y)*sin(y)+sin(x)^cos(y)*sin(y)*log(sin(x))*cos(y)*cos(x)^2/sin(x)^2+
```

$$\sin(x) \cos(y) \sin(y) \cos(x)^2 / \sin(x)^2$$

得到的 LaTeX 命令为:

```
-\frac {\left( \sin \left( x \right) \right) ^{\cos \left( y \right) } \sin \left( y \right) \ln \left( \sin \left( x \right) \right) \left( \cos \left( y \right) \right) \right) ^{2} \left( \cos \left( x \right) \right) ^{2}}{\left( \sin \left( x \right) \right) ^{2}}}-2\, \left( \frac {\left( \sin \left( x \right) \right) ^{\cos \left( y \right) } \cos \left( y \right) \left( \cos \left( x \right) \right) ^{2} \sin \left( y \right) }{\left( \sin \left( x \right) \right) ^{2}} \right) + \left( \sin \left( x \right) \right) ^{\cos \left( y \right) } \sin \left( y \right) \ln \left( \sin \left( x \right) \right) \cos \left( y \right) + \left( \sin \left( x \right) \right) ^{\cos \left( y \right) } \sin \left( y \right) + \left( \frac {\left( \sin \left( x \right) \right) ^{\cos \left( y \right) } \sin \left( y \right) \ln \left( \sin \left( x \right) \right) \cos \left( y \right) \left( \cos \left( x \right) \right) ^{2}}{\left( \sin \left( x \right) \right) ^{2}} \right) + \left( \frac {\left( \sin \left( x \right) \right) ^{\cos \left( y \right) } \sin \left( y \right) \left( \cos \left( x \right) \right) ^{2}}{\left( \sin \left( x \right) \right) ^{2}} \right) \left( \sin \left( x \right) \right) ^{2}}
```

例8 (复杂应用): 已知 $f(x) = x^{x^x}$, 求 $f'''(x)$.

(1) Matlab 命令: (注意不可写成: `diff(x^x^x,x,3)`, 为什么?)
`diff(x^(x^(x^x)),x,3)`

(2) Matlab 结果:

```
x^(x^(x^x))*(x^(x^x))*(x^x*(log(x)+1)*log(x)+x^x/x)*log(x)+x^(x^x)/x)^3+3*x^(x^(x^x))*(x^(x^x))*(x^x*(log(x)+1)*log(x)+x^x/x)*log(x)+x^(x^x)/x)*(x^(x^x))*(x^x*(log(x)+1)*log(x)+x^x/x)^2*log(x)+x^(x^x)*(x^x*(log(x)+1)^2*log(x)+x^x/x*log(x)+2*x^x*(log(x)+1)/x-x^x/x^2)*log(x)+2*x^(x^x)*(x^x*(log(x)+1)*log(x)+x^x/x)/x-x^(x^x)/x^2)+x^(x^(x^x))*(x^(x^x))*(x^x*(log(x)+1)*log(x)+x^x/x)^3*log(x)+3*x^(x^x)*(x^x*(log(x)+1)*log(x)+x^x/x)*log(x)*(x^x*(log(x)+1)^2*log(x)+x^x/x*log(x)+2*x^x*(log(x)+1)/x-x^x/x^2)+3*x^(x^x)*(x^x*(log(x)+1)*log(x)+x^x/x)^2/x+x^(x^x)*(x^x*(log(x)+1)^3*log(x)+3*x^x*(log(x)+1)*log(x)/x+3*x^x*(log(x)+1)^2/x-x^x/x^2*log(x)+3*x^x/x^2-3*x^x*(log(x)+1)/x^2+2*x^x/x^3)*log(x)+3*x^(x^x)*(x^x*(log(x)+1)^2*log(x)+x^x/x*log(x)+2*x^x*(log(x)+1)/x-x^x/x^2)/x-3*x^(x^x)*(x^x*(log(x)+1)*log(x)+x^x/x)/x^2+2*x^(x^x)/x^3)
```

(3) LaTeX 命令 1 (原始程序):

```
{x}^{\left\{ {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \right\} \left( {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \left( {x}^{\left\{ x \right\}} \left( \ln \left( x \right) +1 \right) \right) \ln \left( x \right) +\frac {\left\{ {x}^{\left\{ x \right\}} \right\} {x}}{\left( x \right) } \right) \ln \left( x \right) +\frac {\left\{ {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \right\} {x}}{\left( x \right) } \right) ^{3}+3\, \left\{ {x}^{\left\{ {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \right\}} \right\} \left( {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \left( {x}^{\left\{ x \right\}} \left( \ln \left( x \right) +1 \right) \right) \ln \left( x \right) +\frac {\left\{ {x}^{\left\{ x \right\}} \right\} {x}}{\left( x \right) } \right) \ln \left( x \right) +\frac {\left\{ {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \right\} {x}}{\left( x \right) } \right) \left( {x}^{\left\{ {x}^{\left\{ x \right\}} \right\}} \left( {x}^{\left\{ x \right\}} \left( \ln \left( x \right) +1 \right) \right) \ln \left( x \right) +\frac {\left\{ {x}^{\left\{ x \right\}} \right\} {x}}{\left( x \right) } \right) \right)
```


$$\begin{aligned}
& x^{x^{x^x}} \left(x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right) \ln(x) + \frac{x^{x^x}}{x} \right)^3 + \\
& 3 x^{x^{x^x}} \left(x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right) \ln(x) + \frac{x^{x^x}}{x} \right) \\
& \left(x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right)^2 \ln(x) + x^{x^x} \left(x^x (\ln(x) + 1)^2 \ln(x) + \frac{x^x \ln(x)}{x} + \right. \right. \\
& \left. \left. 2 \frac{x^x (\ln(x) + 1)}{x} - \frac{x^x}{x^2} \right) \ln(x) + 2 x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right) x^{-1} - \frac{x^{x^x}}{x^2} \right) \\
& + x^{x^{x^x}} \left(x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right)^3 \ln(x) + 3 x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right) \right. \\
& \left. \ln(x) \left(x^x (\ln(x) + 1)^2 \ln(x) + \frac{x^x \ln(x)}{x} + 2 \frac{x^x (\ln(x) + 1)}{x} - \frac{x^x}{x^2} \right) \right. \\
& \left. + 3 x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right)^2 x^{-1} + x^{x^x} \left(x^x (\ln(x) + 1)^3 \ln(x) + 3 \frac{x^x (\ln(x) + 1) \ln(x)}{x} \right. \right. \\
& \left. \left. + 3 \frac{x^x (\ln(x) + 1)^2}{x} - \frac{x^x \ln(x)}{x^2} + 3 \frac{x^x}{x^2} - 3 \frac{x^x (\ln(x) + 1)}{x^2} + 2 \frac{x^x}{x^3} \right) \right. \\
& \left. \ln(x) + 3 x^{x^x} \left(x^x (\ln(x) + 1)^2 \ln(x) + \frac{x^x \ln(x)}{x} + 2 \frac{x^x (\ln(x) + 1)}{x} - \frac{x^x}{x^2} \right) x^{-1} - \right. \\
& \left. 3 x^{x^x} \left(x^x (\ln(x) + 1) \ln(x) + \frac{x^x}{x} \right) x^{-2} + 2 \frac{x^{x^x}}{x^3} \right)
\end{aligned}$$

三、练习

分别用 Mathematica 与 Matlab 求解下列数学问题，并给出结果的 LaTeX 源程序和相应的 PDF 文件；

1. 已知函数 $f(x) = \tan^2(x)$ ，求 $f''(x)$ ；
2. 已知函数 $g(x) = \tan(x)^{\cot(x)}$ ，求 $g''(x)$ ；
3. 已知函数 $h(x) = \frac{\tan(x)^{\cot(x)}}{\sin(x)^{\cos(x)}}$ ，求 $h^{(5)}(x)$ ；
4. 已知函数 $l(x, y) = \frac{\tan(x)^{\cot(y)}}{\sin(x)^{\cos(y)}}$ ，求 $\frac{\partial^5 l(x, y)}{\partial x^2 \partial y^3}$ 。